

# GEODESIA

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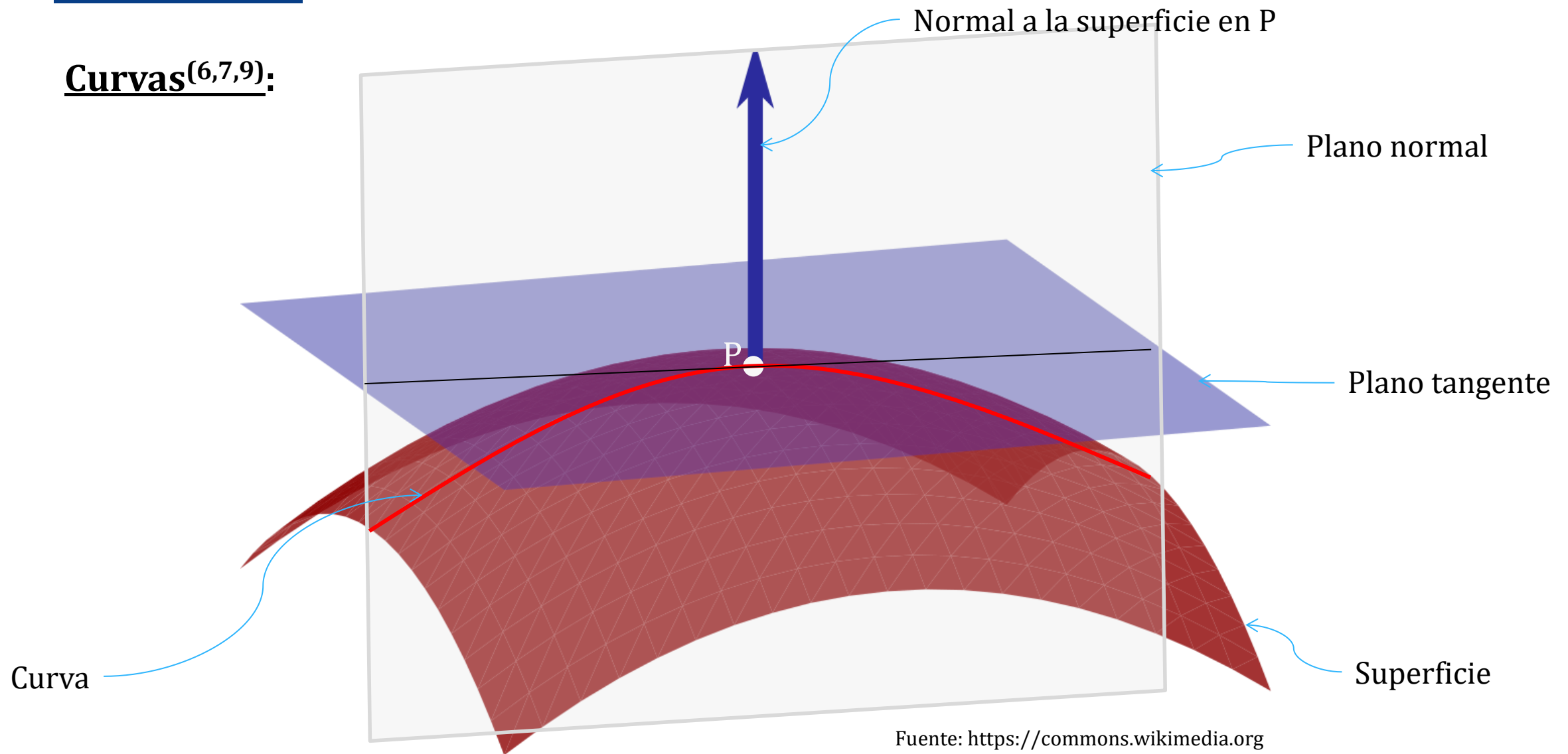
Wilhelm Jordan (1842–1899)  
Handbook of Geodesy



Brigadier Guy Bomford (1899–1996)  
Geodesy

# Geodesia

## Curvas<sup>(6,7,9)</sup>:



Curva de sección normal: es una curva plana creada por la intersección de un plano que contiene la normal a la superficie (un plano de sección normal) con la superficie.

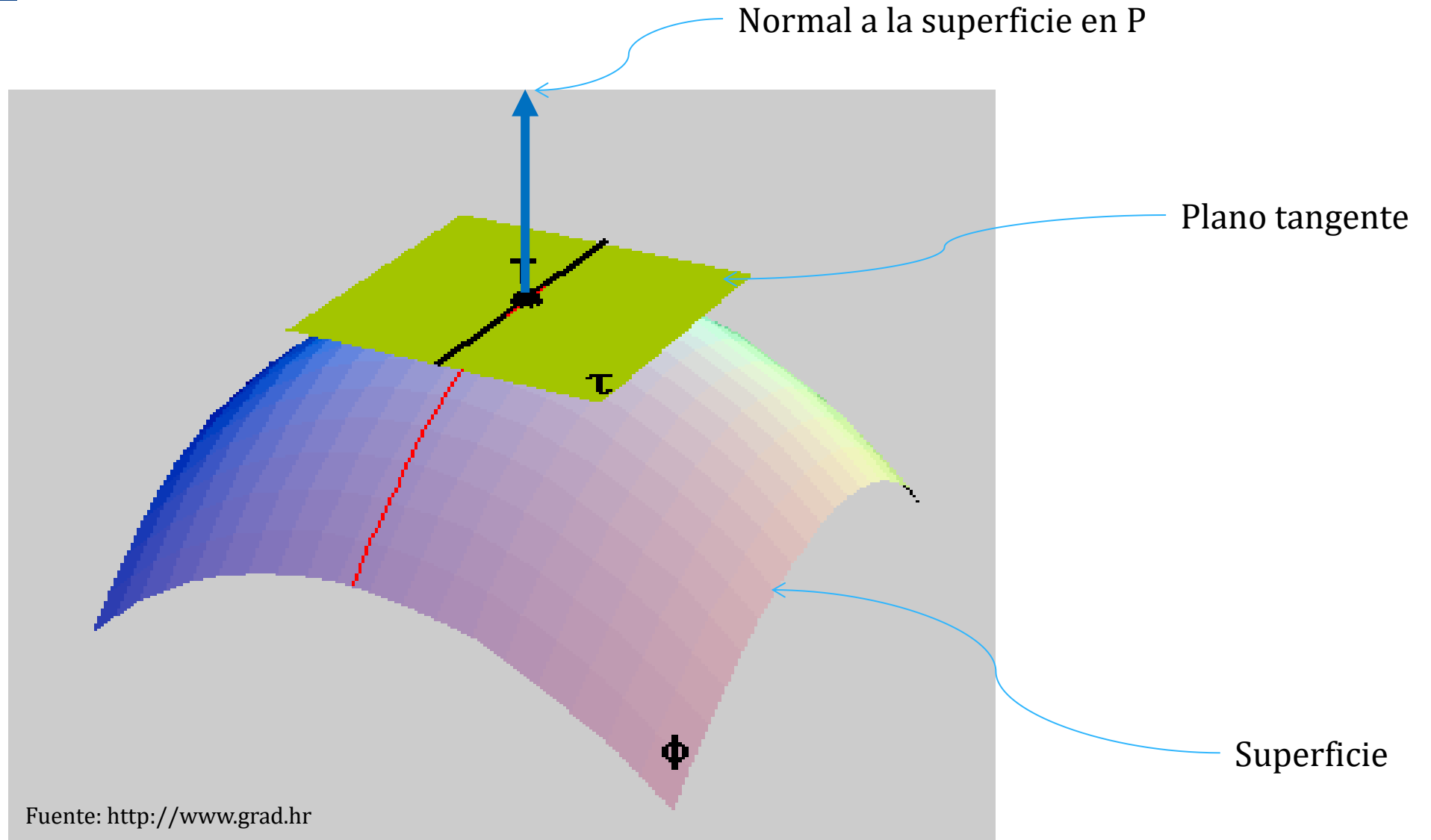
(6) Krakiwsky, Edward J., and Donald B. Thomson (1974). *Geodetic position computations*.. Department of Surveying Engineering, University of New Brunswick.

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## Curvas<sup>(6,7,9)</sup>:



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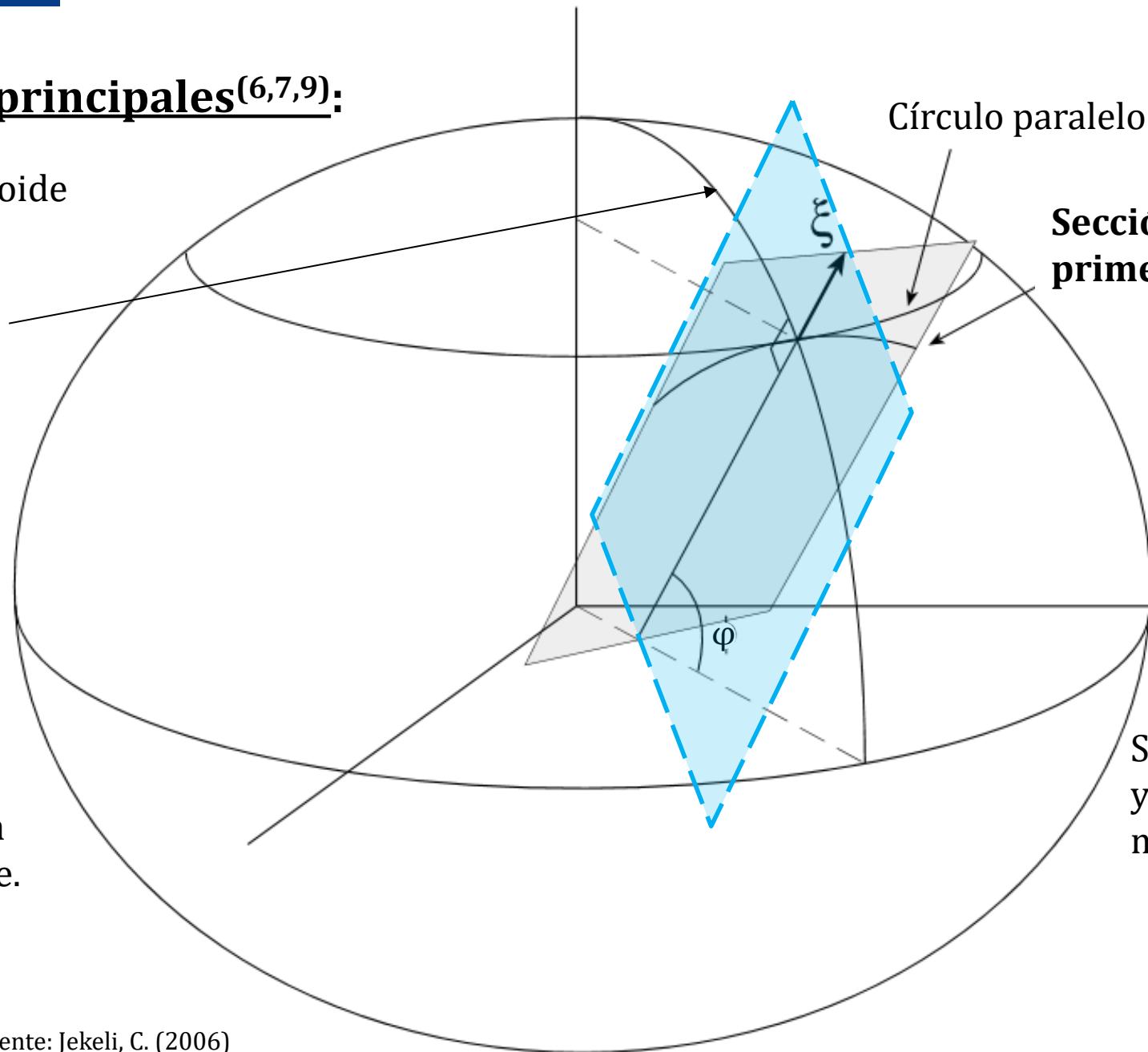
# Geodesia

## Secciones principales<sup>(6,7,9)</sup>:

$\xi$ : Normal al elipsoide

Sección meridiana

Sección que pasa por un punto y contiene a los polos del elipsoide.



Sección que pasa por un punto y es perpendicular a la sección meridiana.

Fuente: Jekeli, C. (2006)

(6) Krakiwsky, Edward J., and Donald B. Thomson (1974). *Geodetic position computations*. Department of Surveying Engineering, University of New Brunswick.

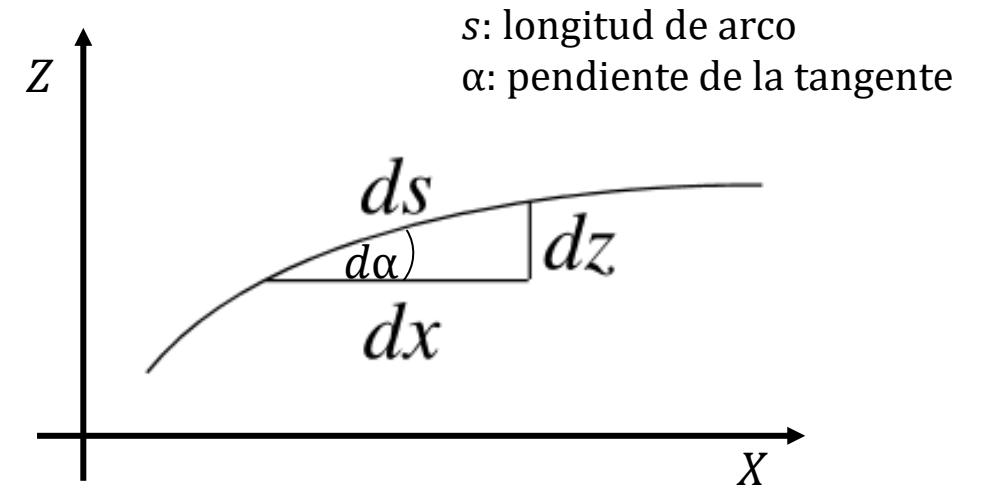
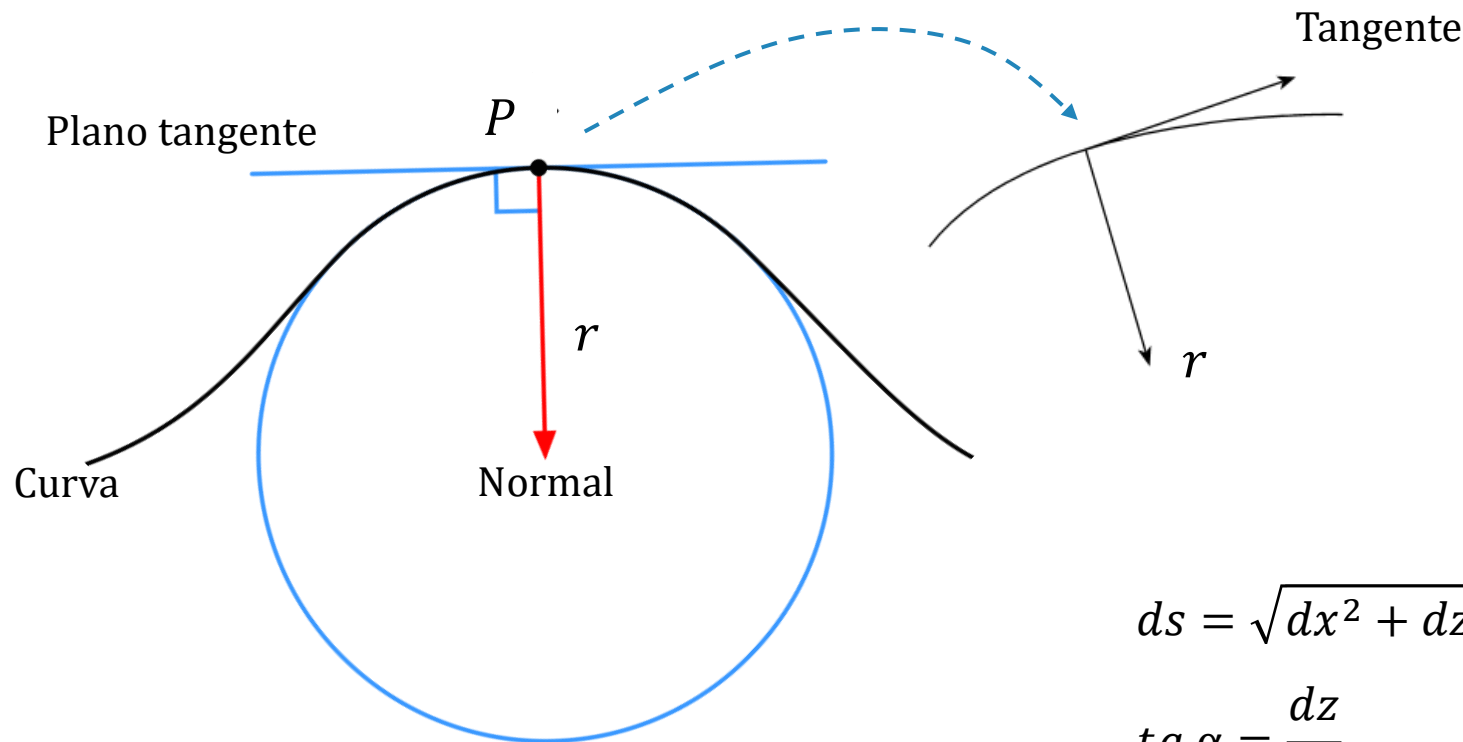
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# Geodesia

**Curvatura**<sup>(6,7,9)</sup>: tasa de cambio absoluta del ángulo de la tangente a la curva respecto a un elemento de longitud de arco de la curva.

$$\chi = \left| \frac{d\alpha}{ds} \right|$$



Fuente: <https://commons.wikimedia.org>  
<https://solitaryroad.com/c361.html>

$$ds = \sqrt{dx^2 + dz^2}$$

$$\operatorname{tg} \alpha = \frac{dz}{dx}$$

$$\chi = \frac{\left| \frac{d^2z}{dx^2} \right|}{\left( 1 + \left( \frac{dz}{dx} \right)^2 \right)^{3/2}}$$

**Radio de Curvatura**: inversa de la curvatura.  $\rho = \frac{1}{\chi}$

**Curvatura**: “es una medida de cuánto se aparta una curva de ser recta”

(6) Krakiwsky, Edward J., and Donald B. Thomson (1974). *Geodetic position computations*. Department of Surveying Engineering, University of New Brunswick.

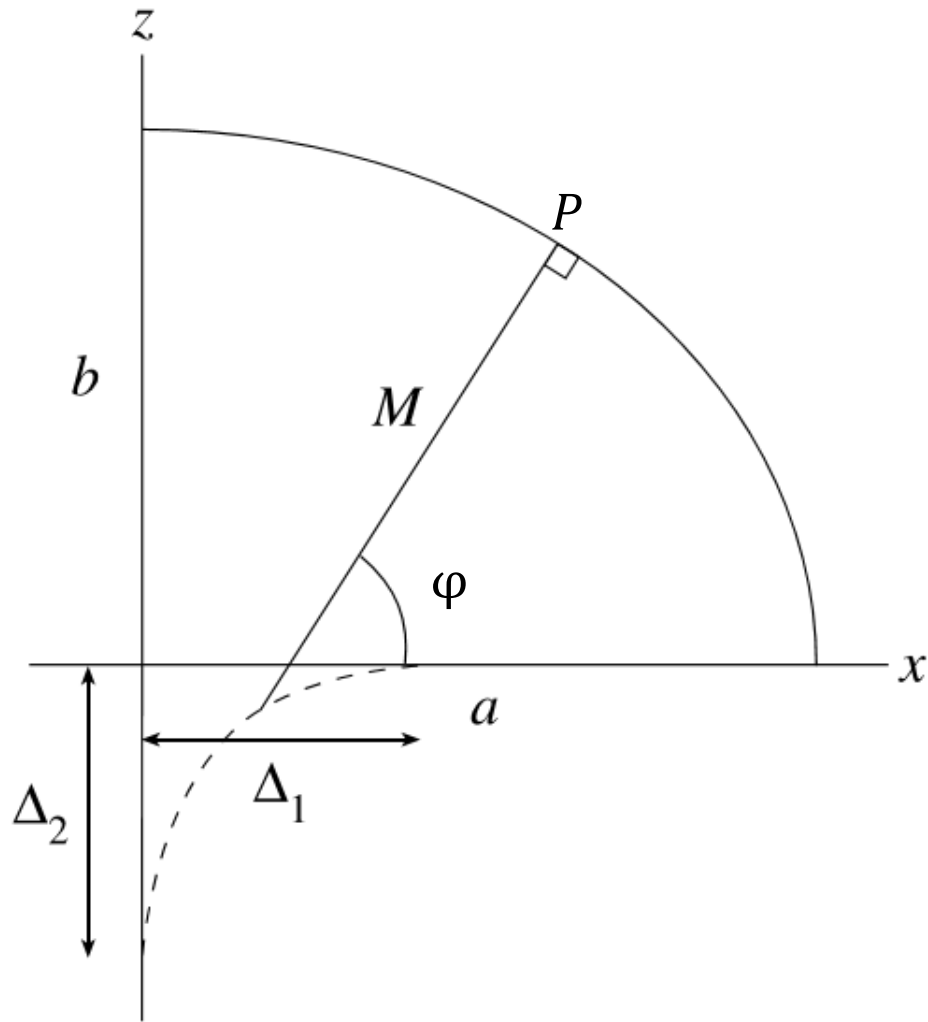
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# Geodesia

## Radio de curvatura<sup>(6,7,9)</sup>:

Sección Meridiana



Fuente: Jekeli, C. (2006)

$$\chi = \frac{\left| \frac{d^2 z}{dx^2} \right|}{\left( 1 + \left( \frac{dz}{dx} \right)^2 \right)^{3/2}} \quad \left\{ \begin{array}{l} \chi = \frac{a}{b^2} (1 - e^2 \sin^2 \varphi)^{3/2} \\ \frac{1}{\chi} = \rho = \frac{a(1 - e^2)}{(1 - e^2 \sin^2 \varphi)^{3/2}} \end{array} \right.$$

$$\frac{dz}{dx} = -\frac{a^2}{b^2} \frac{x}{z} = -\cot g \varphi$$

$$\chi = \left| \frac{d\alpha}{ds} \right| \rightarrow \frac{1}{M} = \left| \frac{d\varphi}{ds} \right| \Rightarrow ds_{meridiana} = M d\varphi$$

$$\begin{array}{l} \varphi_{ecuador} = ? \Rightarrow M_{ecuador} = \frac{a(1 - e^2)}{(1 - e^2 \sin^2 \varphi)^{3/2}} = ? \\ \varphi_{polo} = ? \Rightarrow M_{polo} = \frac{a(1 - e^2)}{(1 - e^2 \sin^2 \varphi)^{3/2}} = ? \end{array}$$

(6) Krakiwsky, Edward J., and Donald B. Thomson (1974). *Geodetic position computations*. Department of Surveying Engineering, University of New Brunswick.

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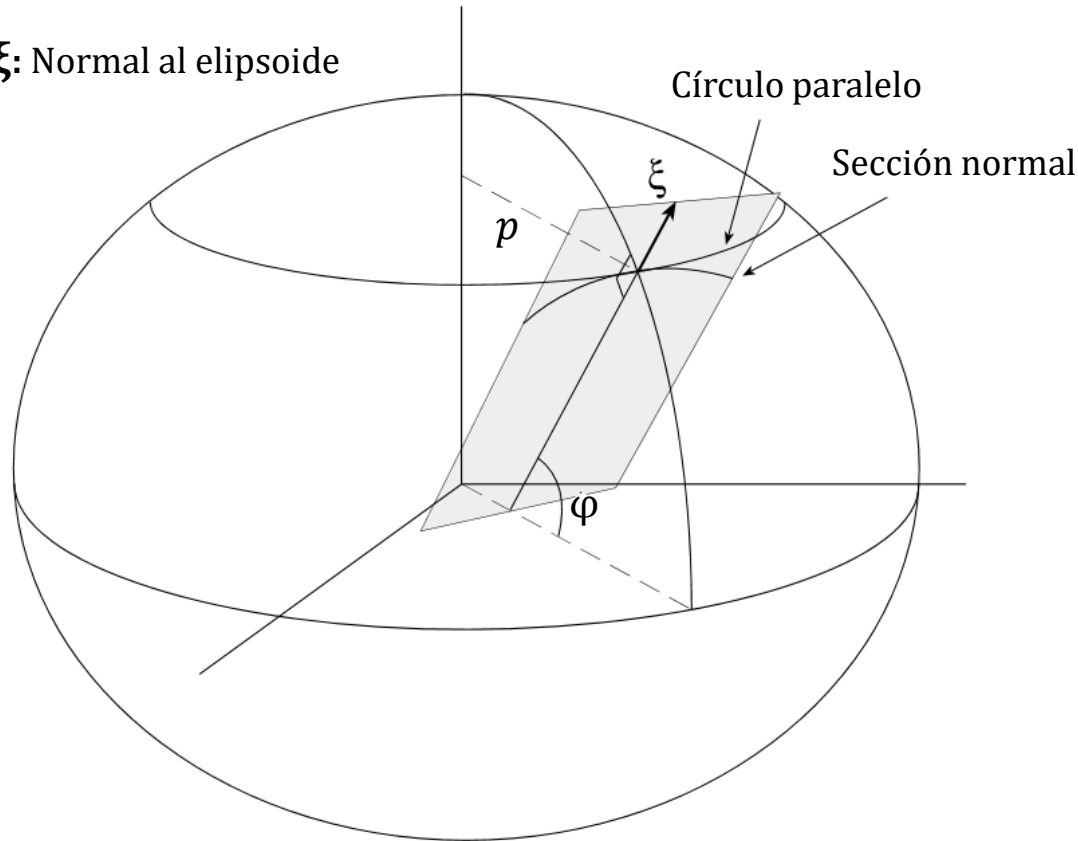
(9) Jekeli, C. (2006). *Geometric reference systems in geodesy*. Division of Geodetic Science, School of Earth Sciences, Ohio State University.

# Geodesia

## Radio de curvatura<sup>(6,7,9)</sup>:

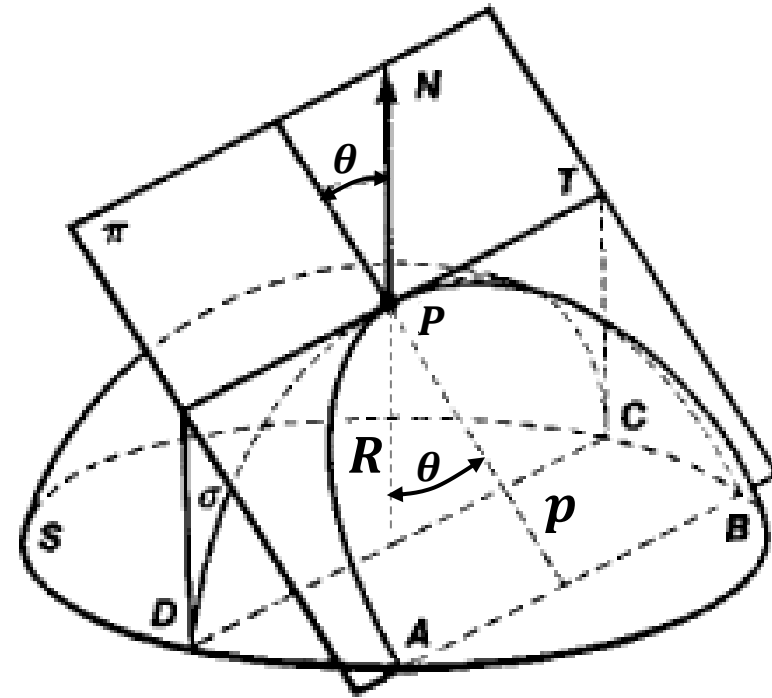
### Sección Normal a la Meridiana

$\xi$ : Normal al elipsoide



Fuente: Jekeli, C. (2006)

Meusnier: el radio de curvatura de una sección inclinada es igual al radio de curvatura de una sección normal multiplicada por el coseno del ángulo entre ambas.



Fuente: <https://encyclopedia2.thefreedictionary.com>

$$p = R \cos \theta \quad \longleftrightarrow \quad \frac{1}{p} \cos \theta = \frac{1}{R}$$

(6) Krakiwsky, Edward J., and Donald B. Thomson (1974). *Geodetic position computations*. Department of Surveying Engineering, University of New Brunswick.

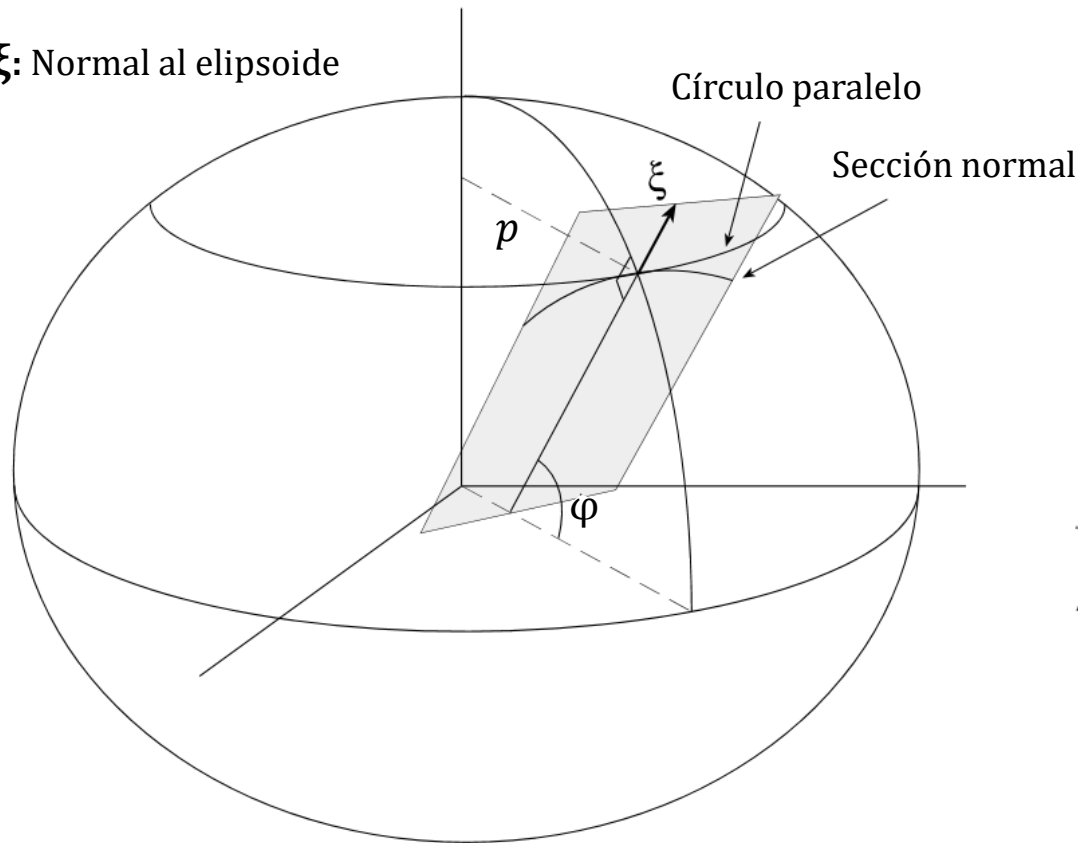
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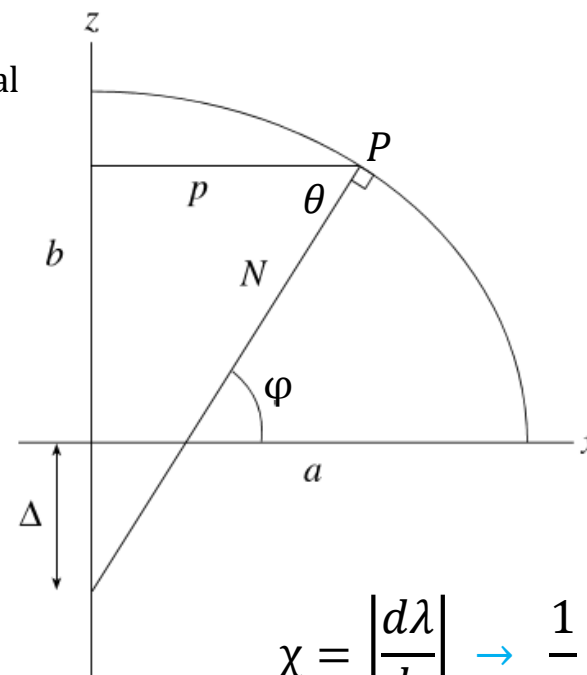
## Radio de curvatura<sup>(6,7,9)</sup>: Sección Normal a la Meridiana

$\xi$ : Normal al elipsoide



Fuente: Jekeli, C. (2006)

Meusnier: el radio de curvatura de una sección inclinada es igual al radio de curvatura de una sección normal multiplicada por el coseno del ángulo entre ambas.



$$\frac{1}{p} \cos \theta = \frac{1}{R} \rightarrow \frac{1}{p} \cos \varphi = \frac{1}{N}$$

$$\left\{ \begin{array}{l} p = N \cos \varphi \\ x = \frac{a \cos \varphi}{(1 - e^2 \sin^2 \varphi)^{1/2}} \end{array} \right.$$

$$N = \frac{a}{(1 - e^2 \sin^2 \varphi)^{1/2}}$$

$$\chi = \left| \frac{d\lambda}{ds} \right| \rightarrow \frac{1}{p} = \left| \frac{d\lambda}{ds} \right| \rightarrow ds_{\text{paralelo}} = N \cos \varphi d\lambda$$

$$\left\{ \begin{array}{l} \varphi_{\text{ecuador}} = ? \rightarrow N_{\text{ecuador}} = \frac{a}{(1 - e^2 \sin^2 \varphi)^{1/2}} = ? \\ \varphi_{\text{polo}} = ? \rightarrow N_{\text{polo}} = \frac{a}{(1 - e^2 \sin^2 \varphi)^{1/2}} = ? \end{array} \right.$$

(6) Krakiwsky, Edward J., and Donald B. Thomson (1974). *Geodetic position computations*. Department of Surveying Engineering, University of New Brunswick.

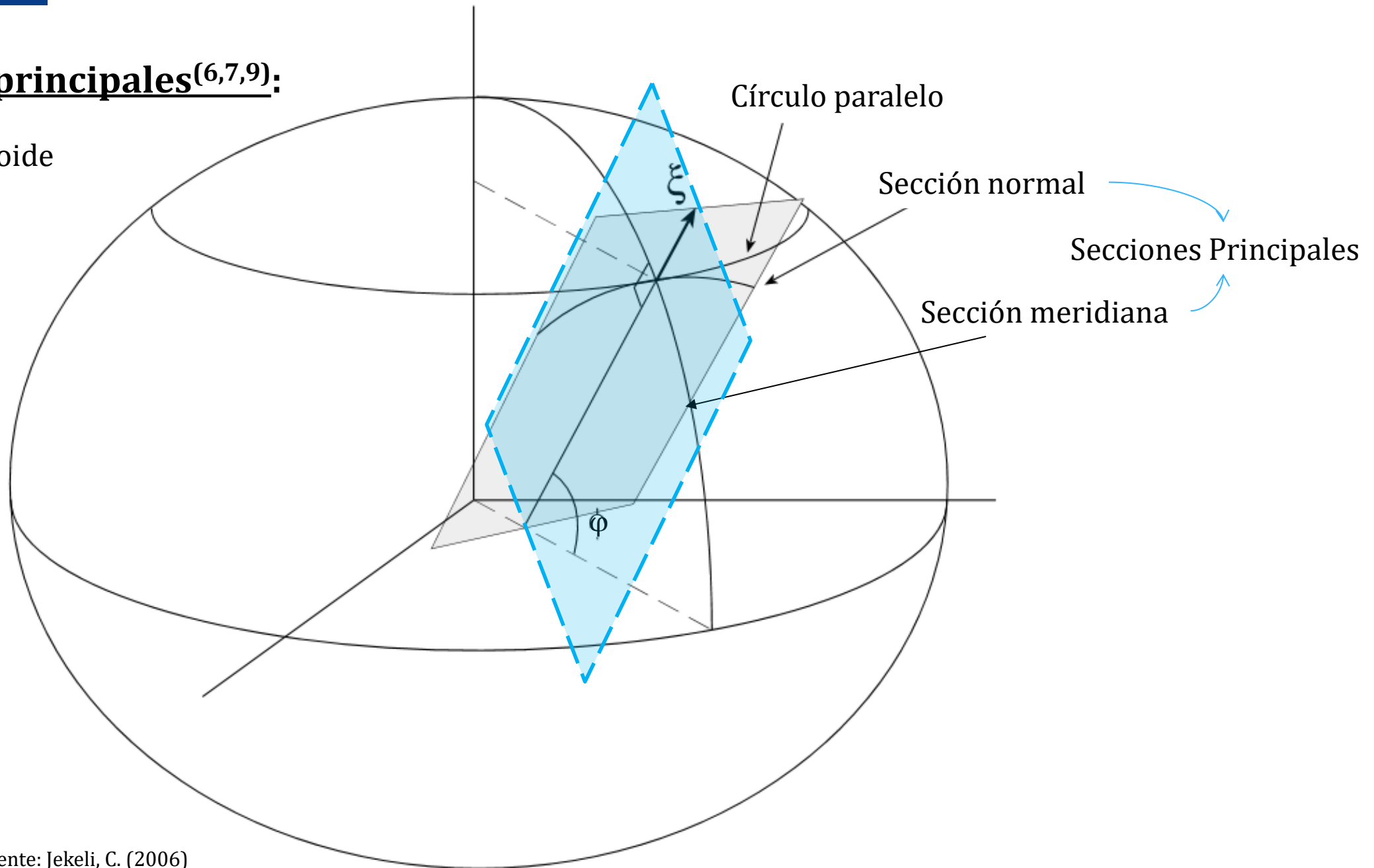
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$\xi$ : Normal al elipsoide



Fuente: Jekeli, C. (2006)

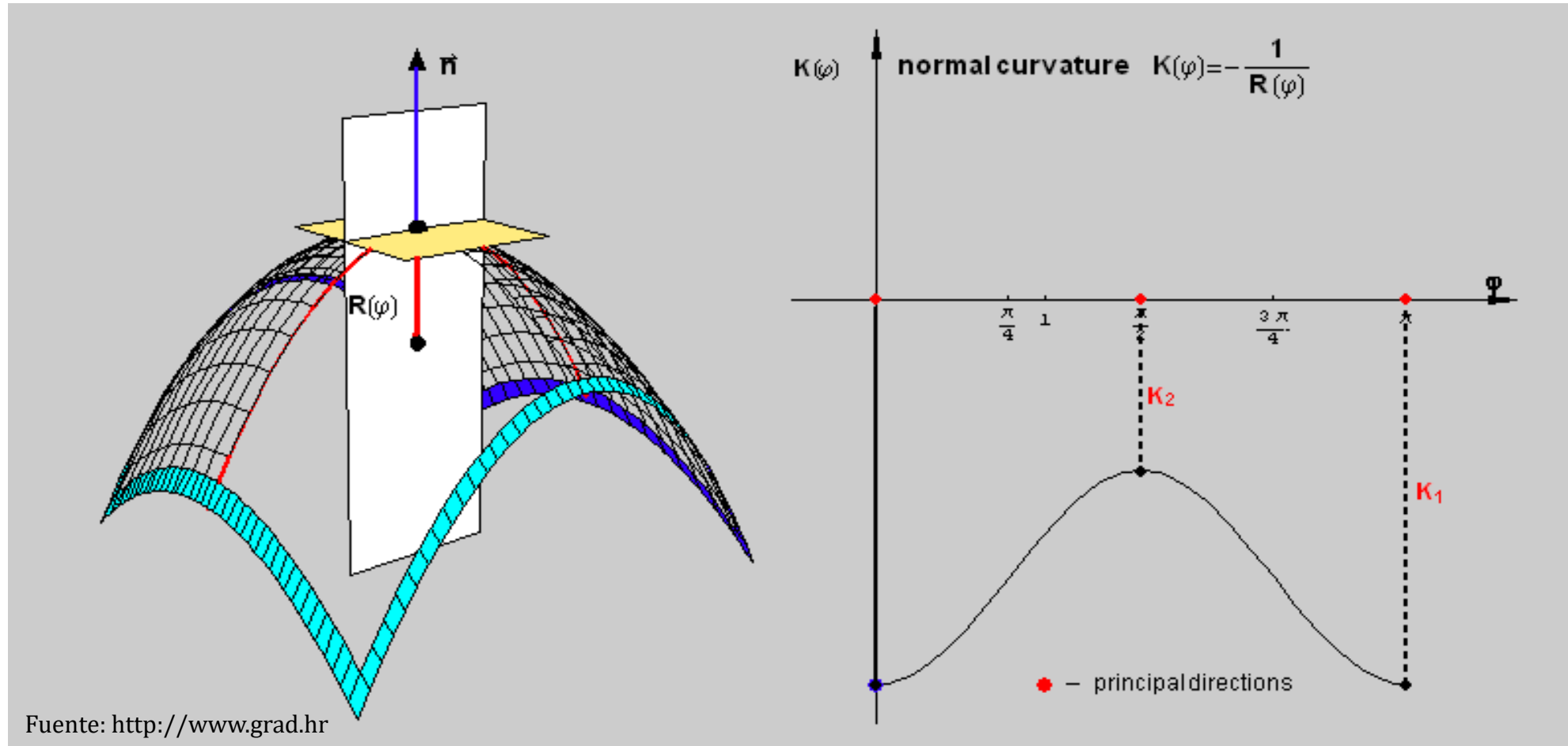
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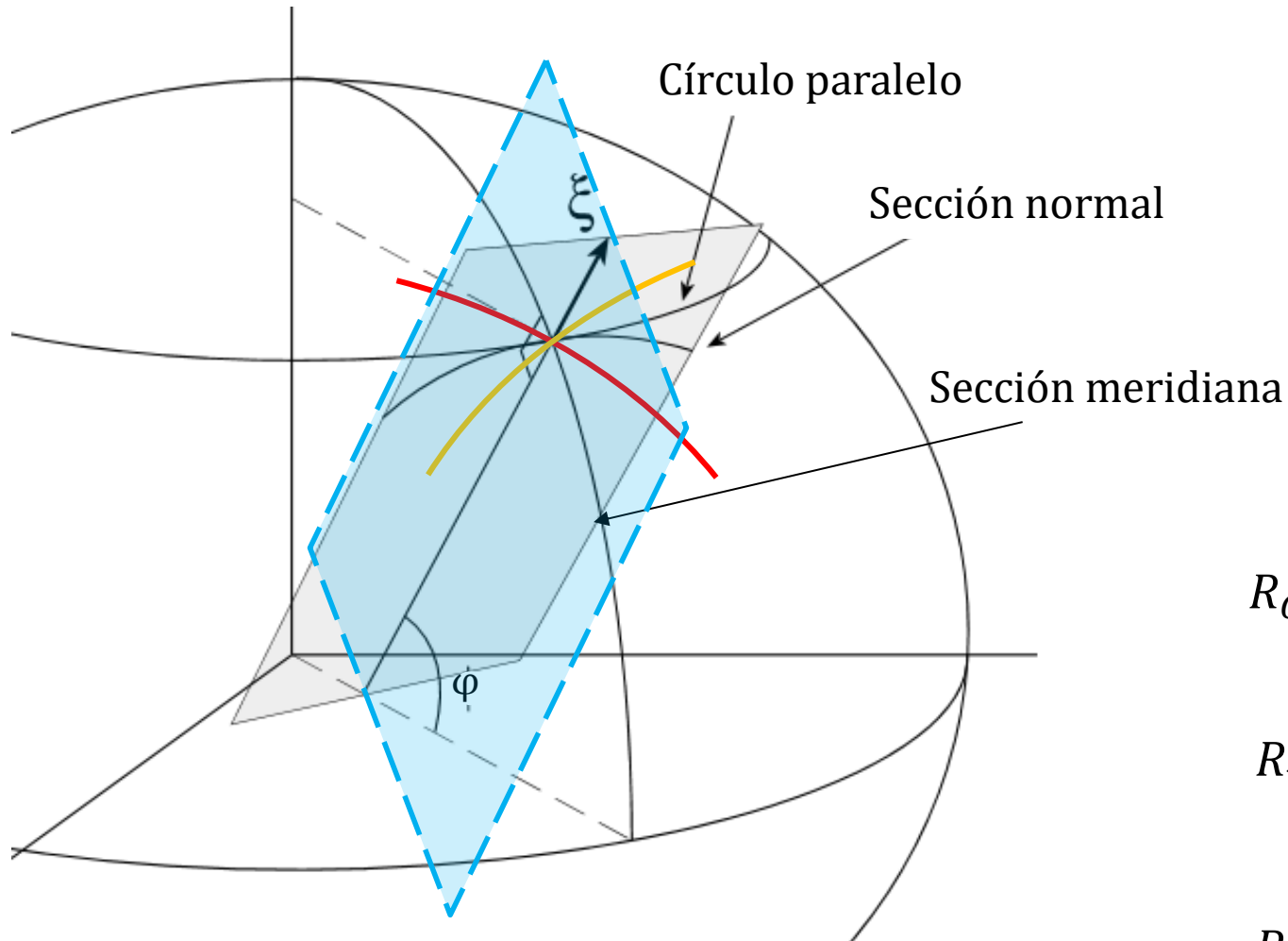
## Curvatura y Radio de Curvatura (6,7,9):



# Geodesia

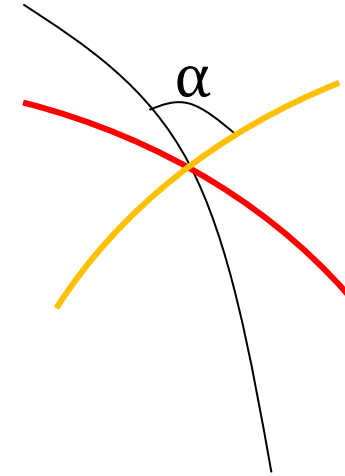
## Curvas en el elipsoide<sup>(6,7,9)</sup>:

$\xi$ : Normal al elipsoide



Fuente: Jekeli, C. (2006)

Teorema de Euler: curvatura de una sección de acimut  $\alpha$  en función de los radio de curvaturas de las secciones principales.



$$\chi_\alpha = \frac{1}{R_\alpha} = \frac{\sin^2 \alpha}{N} + \frac{\cos^2 \alpha}{M}$$

### Aproximaciones

$$R_G = \frac{1}{2\pi} \int_0^{2\pi} R_\alpha d\alpha = \int_0^{2\pi} \frac{d\alpha}{\frac{\sin^2 \alpha}{N} + \frac{\cos^2 \alpha}{M}} = \sqrt{MN}$$

$$R_m = \frac{1}{\frac{1}{2} \left( \frac{1}{N} + \frac{1}{M} \right)}$$

$$R = \frac{1}{3} (a + a + b) \rightarrow R = a \left( 1 - \frac{e^2}{6} - \frac{e^4}{24} - \frac{e^6}{48} - \dots \right)$$

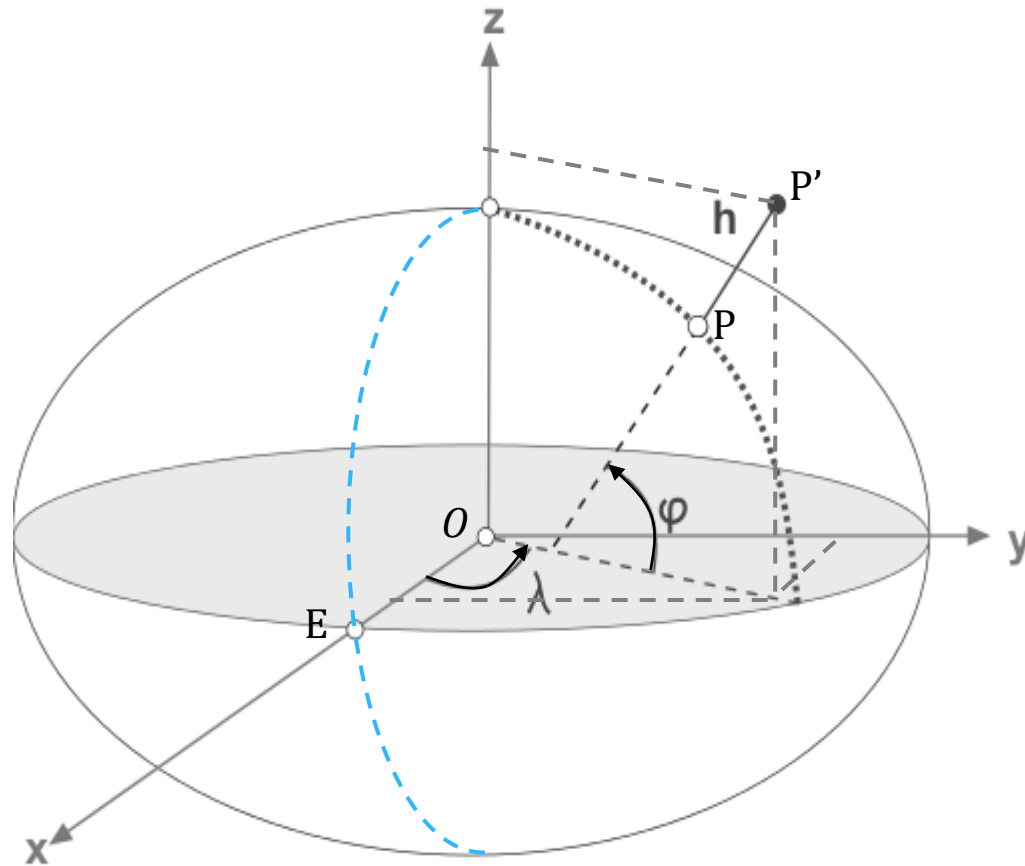
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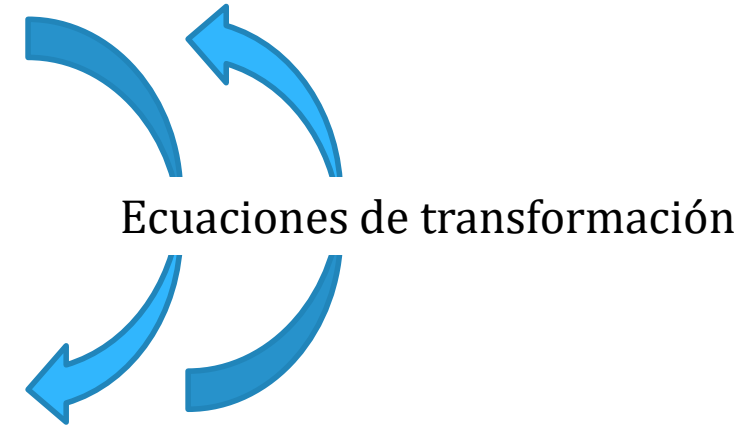
# Geodesia

## Coordenadas Cartesianas Rectangulares<sup>(6,7,9)</sup> asociadas al elipsoide de referencia



$\left. \begin{array}{l} OX \\ OY \\ OZ \end{array} \right\}$  Sistema de la mano derecha

$\left. \begin{array}{l} \varphi \\ \lambda \end{array} \right\}$  Coordenadas curvilíneas en la superficie del elipsoide  
 $h$ : Altura sobre el elipsoide

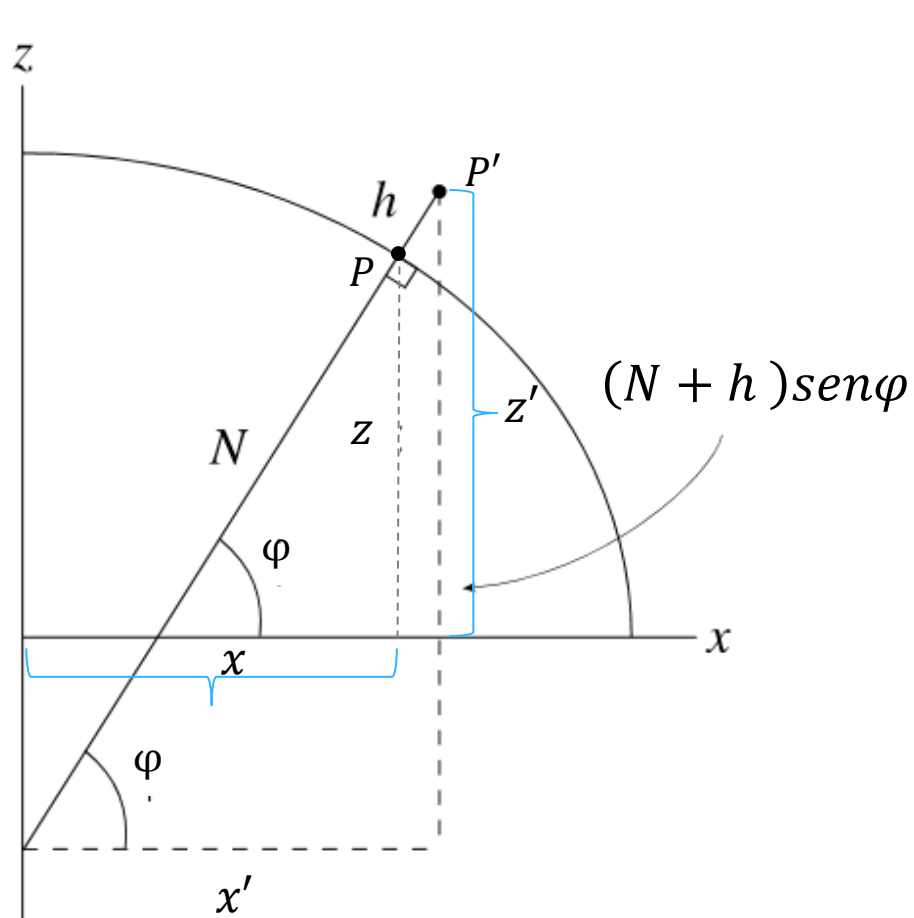


Fuente: <https://gssc.esa.int>  
ESA: European Space Agency

(6) Krakiwsky, Edward J., and Donald B. Thomson (1974). *Geodetic position computations*. Department of Surveying Engineering, University of New Brunswick.  
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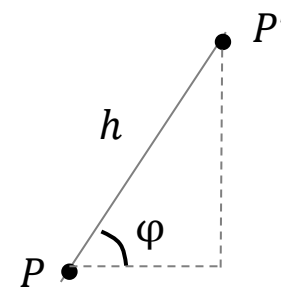
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## Coordenadas Cartesianas Rectangulares<sup>(6,7,9)</sup> asociadas al elipsoide de referencia



Fuente: Jekeli, C. (2006)

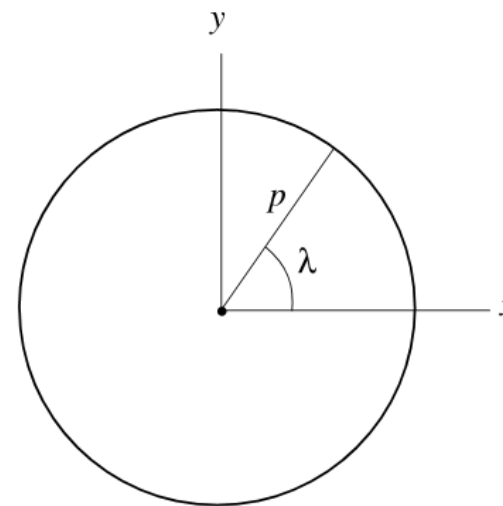
Obtención de  $x$  y  $z$  del punto  $P$



$$x' = x + h \cos \varphi$$

$$z' = z + h \sin \varphi$$

$$\left\{ \begin{array}{l} x = \frac{a \cos \varphi}{(1 - e^2 \sin^2 \varphi)^{1/2}} \\ z = \frac{a (1 - e^2) \sin \varphi}{(1 - e^2 \sin^2 \varphi)^{1/2}} \end{array} \right.$$



$$x' = (x + h \cos \varphi) \cos \lambda$$

$$y' = (y + h \cos \varphi) \sin \lambda$$

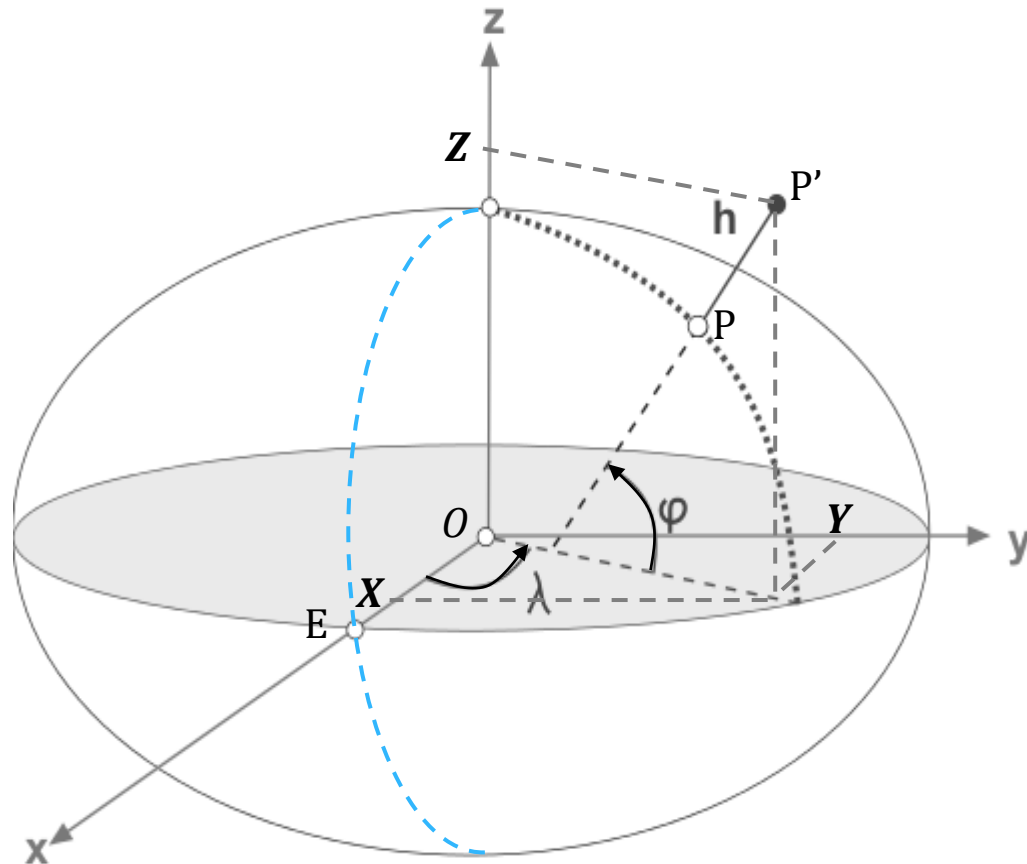
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# Geodesia

## Coordenadas Cartesianas Rectangulares<sup>(6,7,9)</sup> asociadas al elipsoide de referencia



$$N = \frac{a}{(1 - e^2 \sin^2 \varphi)^{1/2}}$$

$$x = \frac{a \cos \varphi}{(1 - e^2 \sin^2 \varphi)^{1/2}}$$

$$z = \frac{a (1 - e^2) \sin \varphi}{(1 - e^2 \sin^2 \varphi)^{1/2}}$$

$$x' = (x + h \cos \varphi) \cos \lambda$$

$$y' = (y + h \cos \varphi) \sin \lambda$$

$$z' = z + h \sin \varphi$$

$$\begin{aligned} X &= (N + h) \cos \varphi \cos \lambda \\ Y &= (N + h) \cos \varphi \sin \lambda \\ Z &= (N(1 - e^2) + h) \sin \varphi \end{aligned}$$

Fuente: <https://gssc.esa.int>  
ESA: European Space Agency

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# Geodesia

## Coordenadas Cartesianas Rectangulares<sup>(6,7,9)</sup> asociadas al elipsoide de referencia

$$\left\{ \begin{array}{l} X = (N + h) \cos \varphi \cos \lambda \\ Y = (N + h) \cos \varphi \sin \lambda \\ Z = (N(1 - e^2) + h) \sin \varphi \end{array} \right.$$

$$\left\{ \begin{array}{l} \frac{Y}{X} = \frac{(N + h) \cos \varphi \sin \lambda}{(N + h) \cos \varphi \cos \lambda} \rightarrow \operatorname{tg} \lambda = \frac{Y}{X} \end{array} \right.$$

$$\left\{ \begin{array}{l} \operatorname{tg} \varphi = \frac{(N + h) \sin \varphi}{\sqrt{X^2 + Y^2}} \rightarrow \varphi = \operatorname{tg}^{-1} \left( \frac{Z}{\sqrt{X^2 + Y^2}} \left( 1 + \frac{N e^2 \sin \varphi}{Z} \right) \right) \end{array} \right.$$

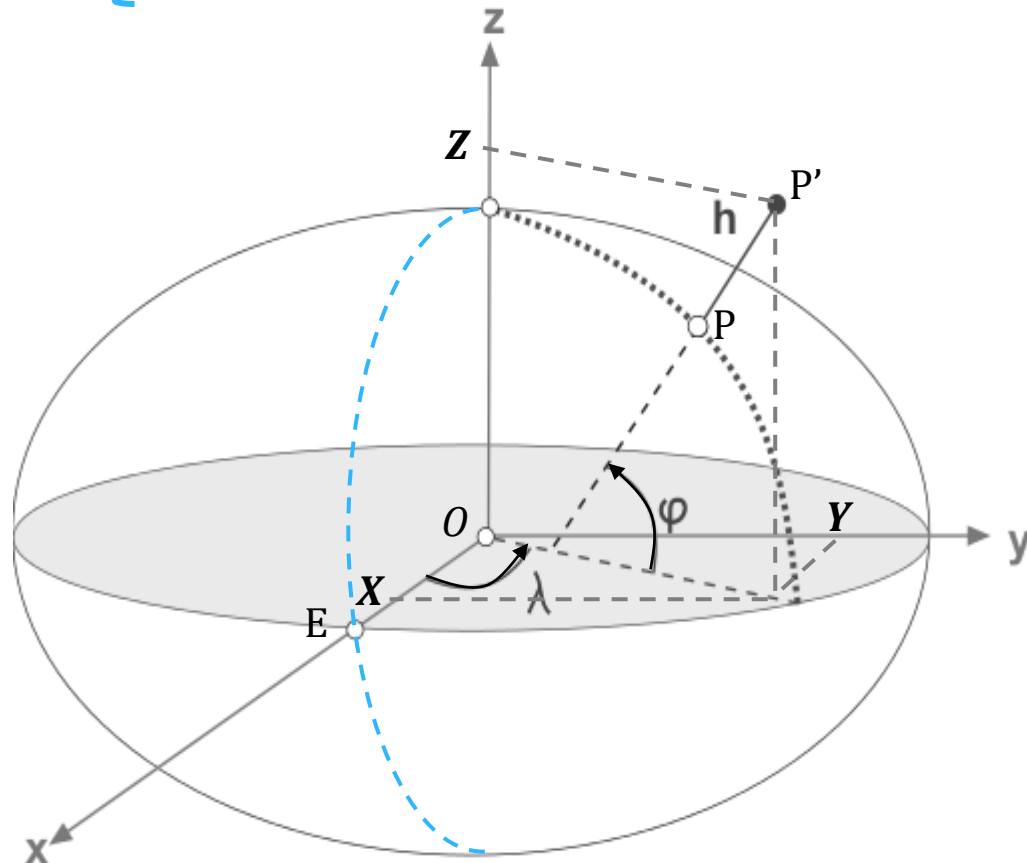
Si  $\rightarrow h = 0$

$$\left\{ \begin{array}{l} \varphi^0 = \operatorname{tg}^{-1} \left( \frac{Z}{\sqrt{X^2 + Y^2}} \left( 1 + \frac{e^2}{1 - e^2} \right) \right) \end{array} \right.$$

$$\left\{ \begin{array}{l} \varphi^1 = \operatorname{tg}^{-1} \left( \frac{Z}{\sqrt{X^2 + Y^2}} \left( 1 + \frac{N(\varphi^0) e^2 \sin \varphi^0}{Z} \right) \right), \quad n \text{ iteraciones} \end{array} \right.$$

$$\left\{ \begin{array}{l} \sqrt{X^2 + Y^2} = (N + h) \cos \varphi \rightarrow h = \frac{\sqrt{X^2 + Y^2}}{\cos \varphi} - N, \quad \text{si } \varphi \neq 90^\circ \end{array} \right.$$

$$\left\{ \begin{array}{l} Z = (N(1 - e^2) + h) \sin \varphi \rightarrow h = \frac{Z}{\sin \varphi} - N(1 - e^2), \quad \text{si } \varphi \neq 0^\circ \end{array} \right.$$



Fuente: <https://gssc.esa.int>  
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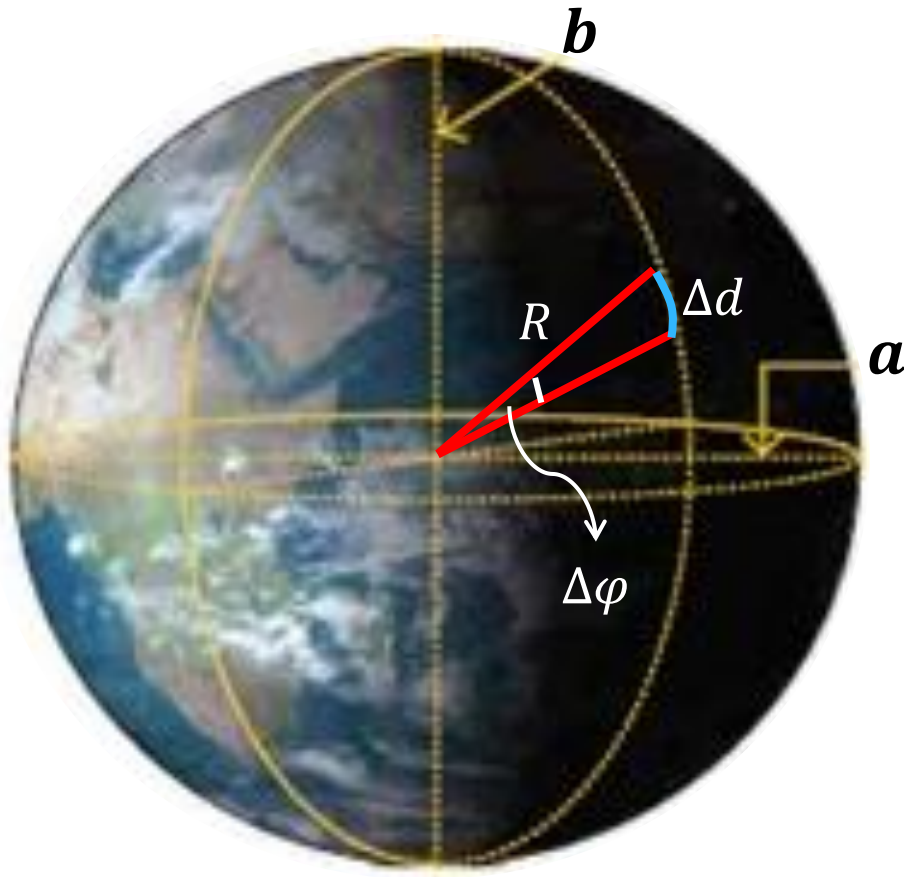
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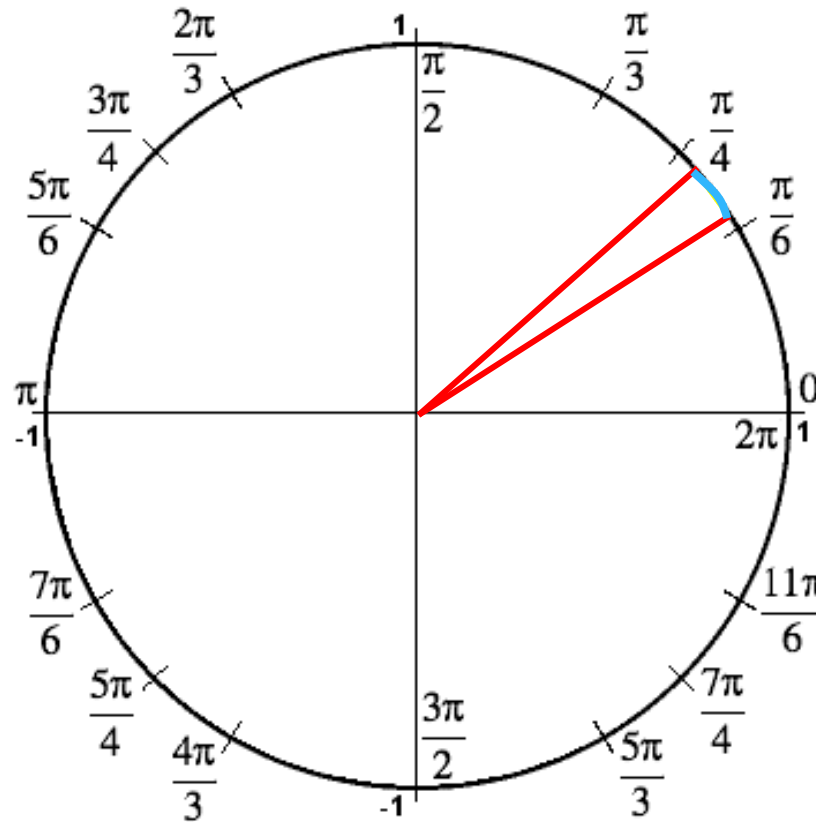
# Geodesia

## Relación de magnitudes<sup>(6,7,9)</sup>

Elipsoide de revolución



Aproximación  $\rightarrow R = \frac{1}{3}(a + a + b) \approx 6371008 \text{ m}$



$$360^\circ \equiv 2\pi R$$

$$360^\circ \equiv 2\pi 6371008 \text{ m}$$

$$1^\circ \approx 111195.066 \dots \text{ m}$$

$$3600'' \approx 111195.066 \text{ m}$$

$$1'' \approx 30.887 \dots \text{ m}$$

$$0.1'' \approx 3.0887 \text{ m}$$

$$0.01'' \approx 0.30887 \text{ m}$$

$$0.001'' \approx$$

Fuente: <https://civilgeeks.com>

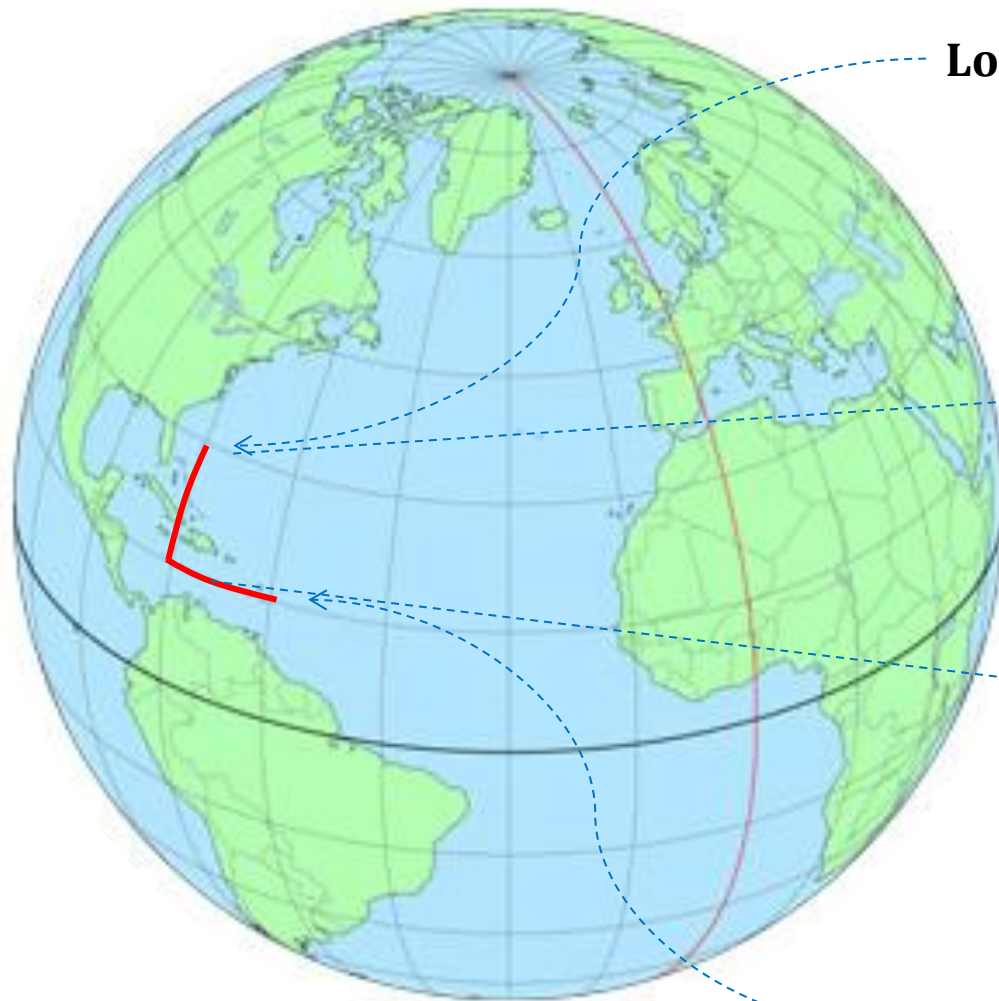
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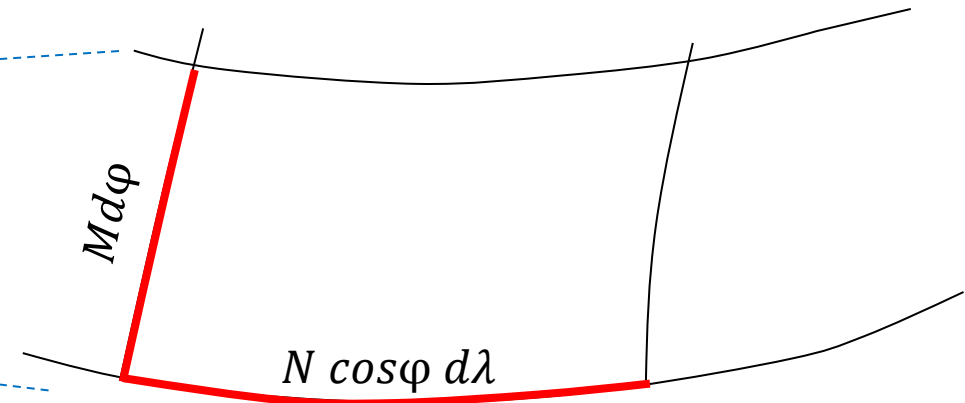
# Geodesia

## Longitudes de arcos<sup>(7,9,10)</sup>:



**Longitud de elemento de Arco de Meridiano**

$$\chi = \left| \frac{d\alpha}{ds} \right| \rightarrow \frac{1}{M} = \left| \frac{d\varphi}{ds} \right| \Rightarrow ds_{\text{meridiana}} = M d\varphi$$



$$\chi = \left| \frac{d\alpha}{ds} \right| \rightarrow \frac{1}{p} = \left| \frac{d\lambda}{ds} \right| \Rightarrow ds_{\text{paralelo}} = N \cos \varphi d\lambda$$

**Longitud de elemento de Arco de Paralelo**

Fuente: [www.thegreenwichmeridian.org](http://www.thegreenwichmeridian.org)

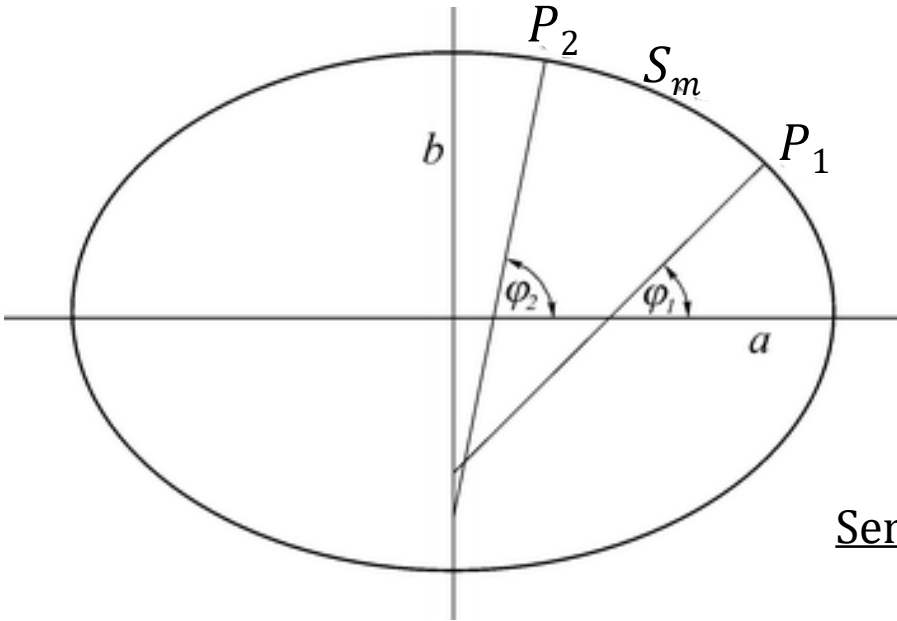
(7) Rapp, Richard H. (1991). *Geometric geodesy part I*. Department of Geodetic Science and Surveying, Ohio State University.

(9) Jekeli, C. (2006). *Geometric reference systems in geodesy*. Division of Geodetic Science, School of Earth Sciences. Ohio State University.

(10) Jordan, W. (1962). *Handbook of Geodesy* (Vol. 3). Corps of Engineers, United States Army, Army Map Service

# Geodesia

## Longitudes de arcos<sup>(7,9,10):</sup>



$$\chi = \left| \frac{d\alpha}{ds} \right| \rightarrow \frac{1}{M} = \left| \frac{d\varphi}{ds} \right| \quad \Rightarrow \quad ds_{\text{meridiana}} = M d\varphi$$

$$S_m = \int_{\varphi_1}^{\varphi_2} M d\varphi = \int_{\varphi_1}^{\varphi_2} \frac{a(1-e^2)}{(1-e^2 \text{sen}^2 \varphi)^{3/2}} d\varphi$$

$$S_m = a(1-e^2) \int_{\varphi_1}^{\varphi_2} (1-e^2 \text{sen}^2 \varphi)^{-3/2} d\varphi \quad \text{Integral elíptica}$$

Series de Maclaurin

$$f(x) = f(x_0) + (x - x_0)f'(x_0) + \frac{(x - x_0)^2}{2!} f''(x_0) + \dots$$

Fuente: Lapaine M. (2017)

$$\frac{1}{(1-e^2 \text{sen}^2 \varphi)^{3/2}} = 1 + \frac{3}{2} e^2 \text{sen}^2 \varphi + \frac{15}{8} e^4 \text{sen}^4 \varphi + \frac{35}{16} e^6 \text{sen}^6 \varphi + \frac{315}{128} e^8 \text{sen}^8 \varphi + \frac{693}{256} e^{10} \text{sen}^{10} \varphi + \dots$$

$$\text{sen}^2 \varphi = \frac{1}{2} - \frac{1}{2} \cos 2\varphi ; \text{sen}^4 \varphi = \frac{3}{8} - \frac{1}{2} \cos 2\varphi + \frac{1}{8} \cos 4\varphi ; \dots$$

$$\frac{1}{(1-e^2 \text{sen}^2 \varphi)^{3/2}} = A - B \cos 2\varphi + C \cos 4\varphi - D \cos 6\varphi + E \cos 8\varphi - F \cos 10\varphi + \dots$$

$$\int \cos 2\varphi d\varphi = \frac{1}{2} \text{sen} 2\varphi$$

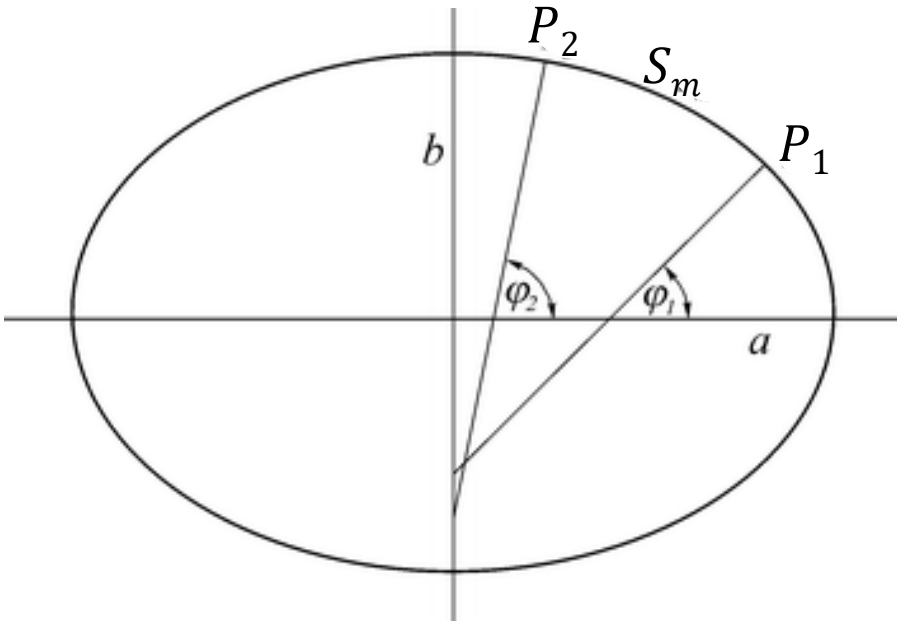
(7) Rapp, Richard H. (1991). *Geometric geodesy part I*. Department of Geodetic Science and Surveying, Ohio State University.

(9) Jekeli, C. (2006). *Geometric reference systems in geodesy*. Division of Geodetic Science, School of Earth Sciences. Ohio State University.

(10) Jordan, W. (1962). *Handbook of Geodesy* (Vol. 3). Corps of Engineers, United States Army, Army Map Service

# Geodesia

## Longitudes de arcos<sup>(7,9,10)</sup>:



Fuente: Lapaine M. (2017)

$$S_m = a(1 - e^2) \left[ A(\varphi_2 - \varphi_1) - \frac{B}{2}(\text{sen}2\varphi_2 - \text{sen}2\varphi_1) + \frac{C}{4}(\text{sen}4\varphi_2 - \text{sen}4\varphi_1) - \frac{D}{6}(\text{sen}6\varphi_2 - \text{sen}6\varphi_1) + \frac{E}{8}(\text{sen}8\varphi_2 - \text{sen}8\varphi_1) - \frac{F}{10}(\text{sen}10\varphi_2 - \text{sen}10\varphi_1) \right]$$

$$A = 1 + \frac{3}{4}e^2 + \frac{45}{64}e^4 + \frac{175}{256}e^6 + \frac{11025}{16384}e^8 + \frac{43659}{65536}e^{10} + \dots$$

$$B = \frac{3}{4}e^2 + \frac{15}{16}e^4 + \frac{525}{512}e^6 + \frac{2205}{2048}e^8 + \frac{72765}{65536}e^{10} + \dots$$

$$C = \frac{15}{64}e^4 + \frac{105}{256}e^6 + \frac{2205}{4096}e^8 + \frac{10395}{16384}e^{10} + \dots$$

$$D = \frac{35}{512}e^6 + \frac{315}{2048}e^8 + \frac{31185}{131072}e^{10} + \dots$$

$$E = \frac{315}{16384}e^8 + \frac{3465}{65536}e^{10} + \dots$$

$$F = \frac{693}{131072}e^{10} + \dots$$

Fuente: Jordan, W. (1962).

Si  $\varphi_1 = 0^\circ \rightarrow$  Longitud de arco desde el ecuador al polo

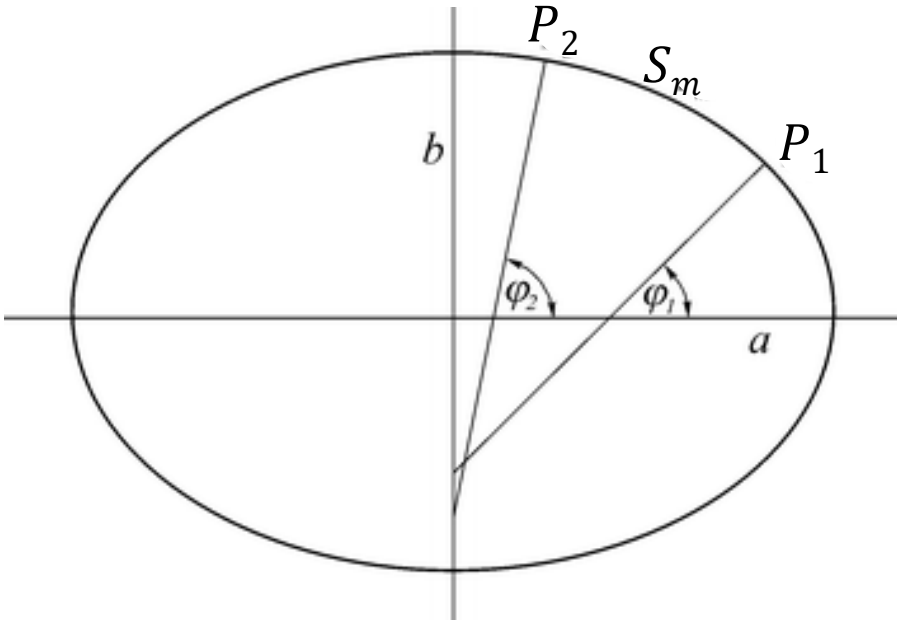
(7) Rapp, Richard H. (1991). *Geometric geodesy part I*. Department of Geodetic Science and Surveying, Ohio State University.

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(10) Jordan, W. (1962). *Handbook of Geodesy* (Vol. 3). Corps of Engineers, United States Army, Army Map Service

# Geodesia

## Longitudes de arcos<sup>(7,9,10)</sup>:



Fuente: Lapaine M. (2017)

Si  $\varphi_1 = 0^\circ \rightarrow$  Longitud de arco desde el ecuador al polo

Helmert

$$S_m = \frac{a}{1+n} [a_0\varphi_2 - a_2\text{sen}2\varphi_2 + a_4\text{sen}4\varphi_2 - a_6\text{sen}6\varphi_2 + a_8\text{sen}8\varphi_2]$$

$$a_0 = 1 + \frac{n^2}{4} + \frac{n^4}{64}$$

$$n = \frac{f}{2-f} = \frac{1-\sqrt{1-e^2}}{1+\sqrt{1-e^2}}$$

$$a_2 = \frac{3}{2} \left( n - \frac{n^3}{8} \right)$$

$$a_4 = \frac{15}{16} \left( n^2 - \frac{n^4}{4} \right)$$

$$a_6 = \frac{35}{45} n^3$$

$$a_8 = \frac{315}{512} n^4$$

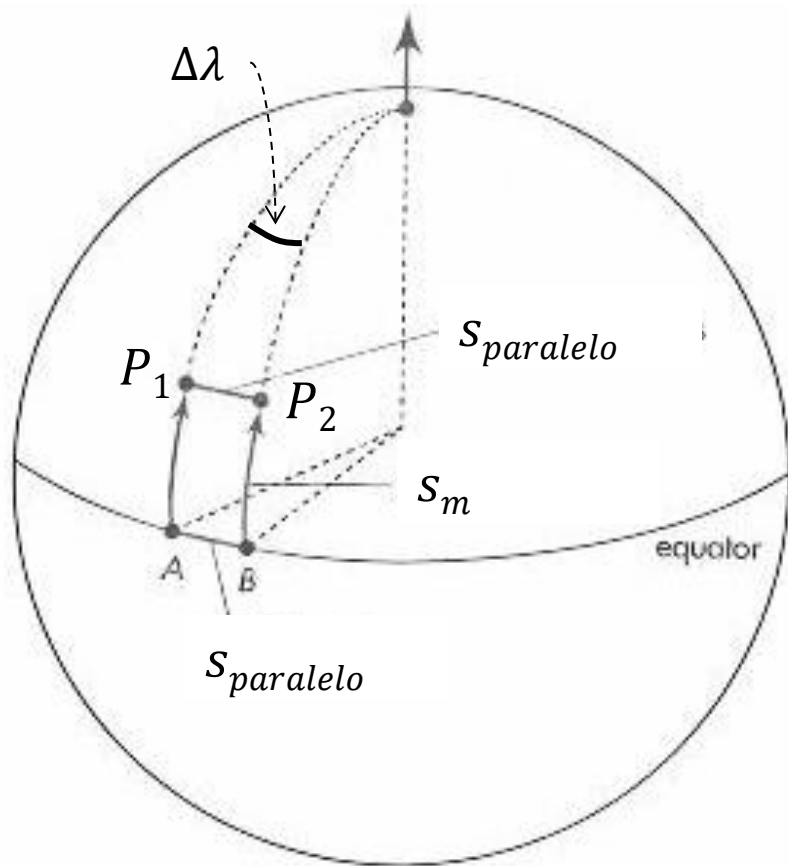
(7) Rapp, Richard H. (1991). *Geometric geodesy part I*. Department of Geodetic Science and Surveying, Ohio State University.

(9) Jekeli, C. (2006). *Geometric reference systems in geodesy*. Division of Geodetic Science, School of Earth Sciences. Ohio State University.

(10) Jordan, W. (1962). *Handbook of Geodesy* (Vol. 3). Corps of Engineers, United States Army, Army Map Service

# Geodesia

## Longitudes de arcos<sup>(7,9,10)</sup>:



$$\chi = \left| \frac{d\alpha}{ds} \right| \rightarrow \frac{1}{p} = \left| \frac{d\lambda}{ds} \right| \Rightarrow ds_{\text{paralelo}} = N \cos \varphi d\lambda$$

$$S_{\text{paralelo}} = N \cos \varphi \Delta\lambda \quad , \quad \Delta\lambda = \lambda_2 - \lambda_1$$

(7) Rapp, Richard H. (1991). *Geometric geodesy part I*. Department of Geodetic Science and Surveying, Ohio State University.

(9) Jekeli, C. (2006). *Geometric reference systems in geodesy*. Division of Geodetic Science, School of Earth Sciences. Ohio State University.

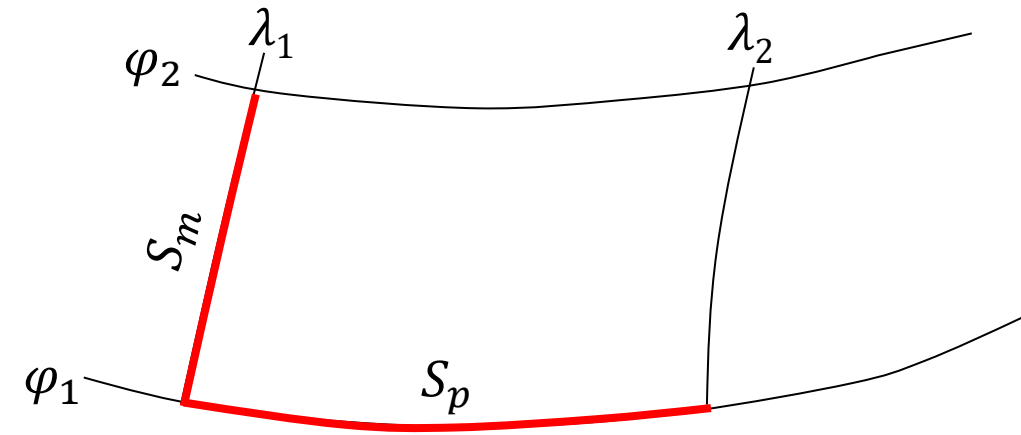
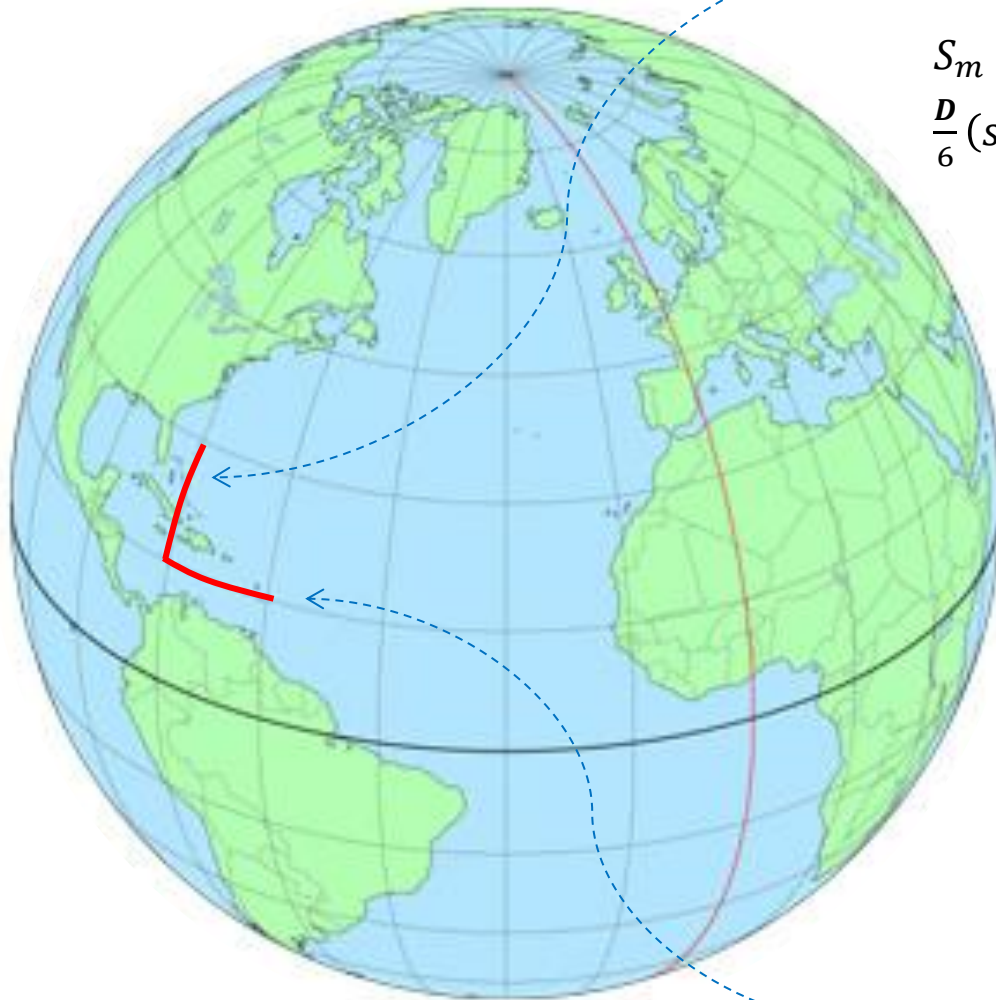
(10) Jordan, W. (1962). *Handbook of Geodesy* (Vol. 3). Corps of Engineers, United States Army, Army Map Service

# Geodesia

## Longitudes de arcos<sup>(7,9,10)</sup>:

### Longitud de Arco de Meridiano

$$S_m = a(1 - e^2) \left[ A(\varphi_2 - \varphi_1) - \frac{B}{2}(\text{sen}2\varphi_2 - \text{sen}2\varphi_1) + \frac{C}{4}(\text{sen}4\varphi_2 - \text{sen}4\varphi_1) - \frac{D}{6}(\text{sen}6\varphi_2 - \text{sen}6\varphi_1) + \frac{E}{8}(\text{sen}8\varphi_2 - \text{sen}8\varphi_1) - \frac{F}{10}(\text{sen}10\varphi_2 - \text{sen}10\varphi_1) \right]$$



### Longitud de Arco de Paralelo $S_p = N \cos\varphi \Delta\lambda$

Fuente: [www.thegreenwichmeridian.org](http://www.thegreenwichmeridian.org)

(7) Rapp, Richard H. (1991). *Geometric geodesy part I*. Department of Geodetic Science and Surveying, Ohio State University.

(9) Jekeli, C. (2006). *Geometric reference systems in geodesy*. Division of Geodetic Science, School of Earth Sciences, Ohio State University.

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